

Analyse statistique des données d'IRMf (avec le logiciel SPM5)

Inserm

Institut national
de la santé et de la recherche médicale

UPMC
PARIS UNIVERSITÉS

CHU-PS
Pitié - Salpêtrière

Tests statistiques, analyse des résultats

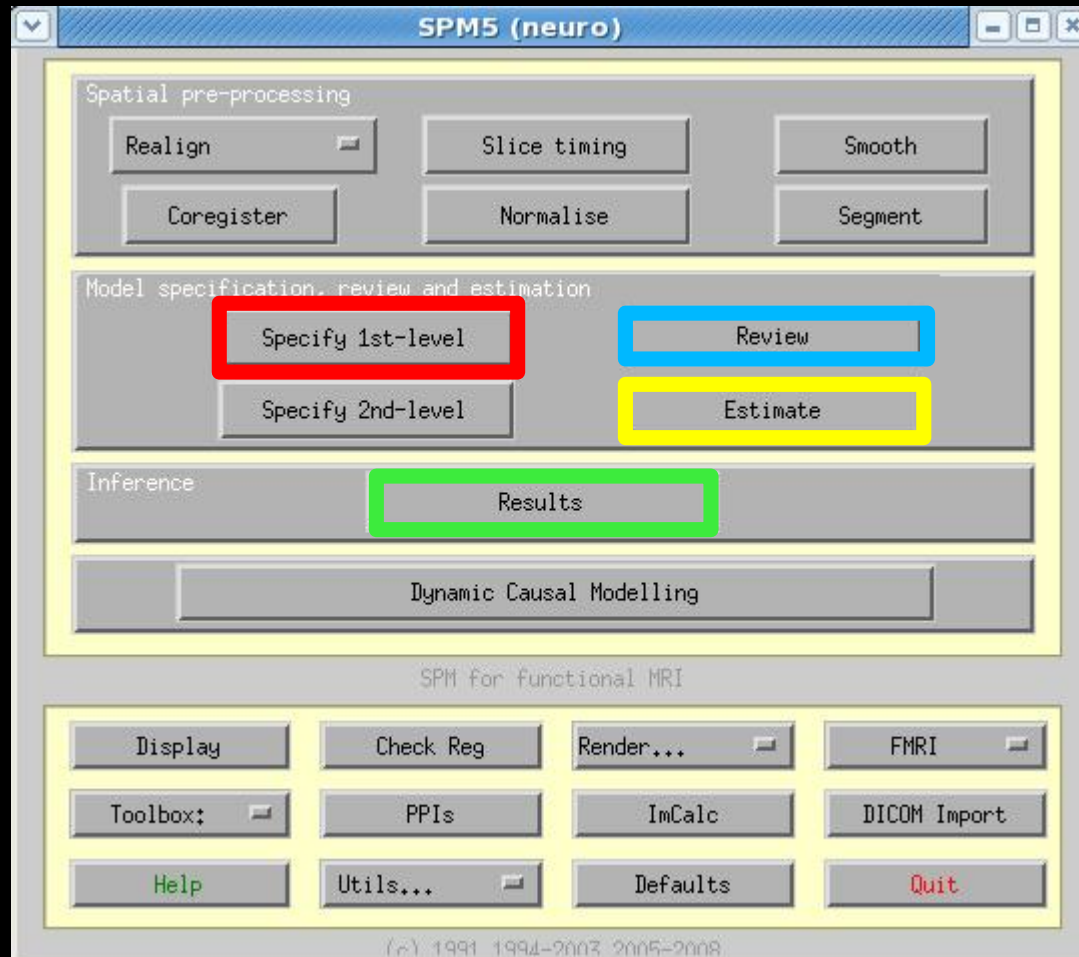
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Melanie.Pelegriani@imed.jussieu.fr



Laboratoire d'Imagerie Fonctionnelle
UMR-S 678 Inserm/UPMC

Analyse de premier niveau



1- Décrire X

4 - Faire des tests (inférence) sur les β

2- Vérifier X

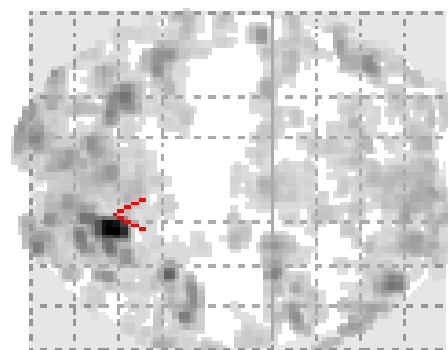
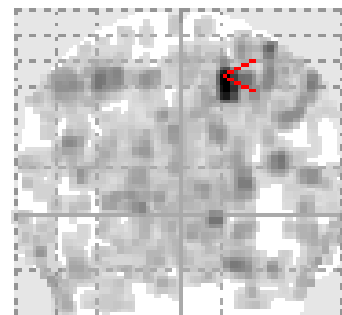
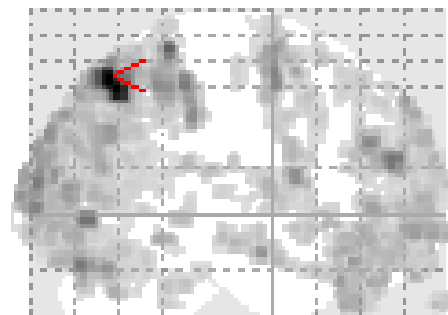
3- Estimer β

ess_0001
spmF_0001

effects of interest

numéro du contraste

SPM_{map}
[20, -64, 50] ← coordonnées du curseur rouge en mm



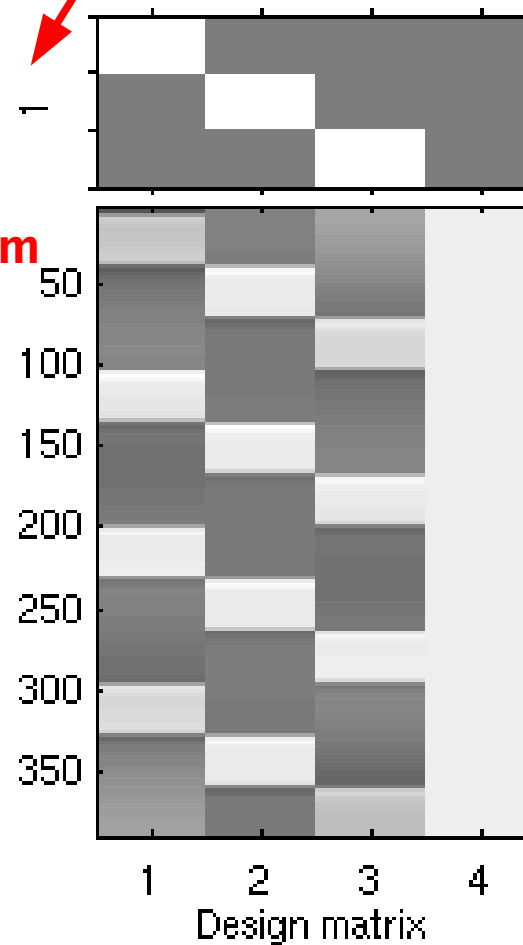
SPM{F_{3,380}}

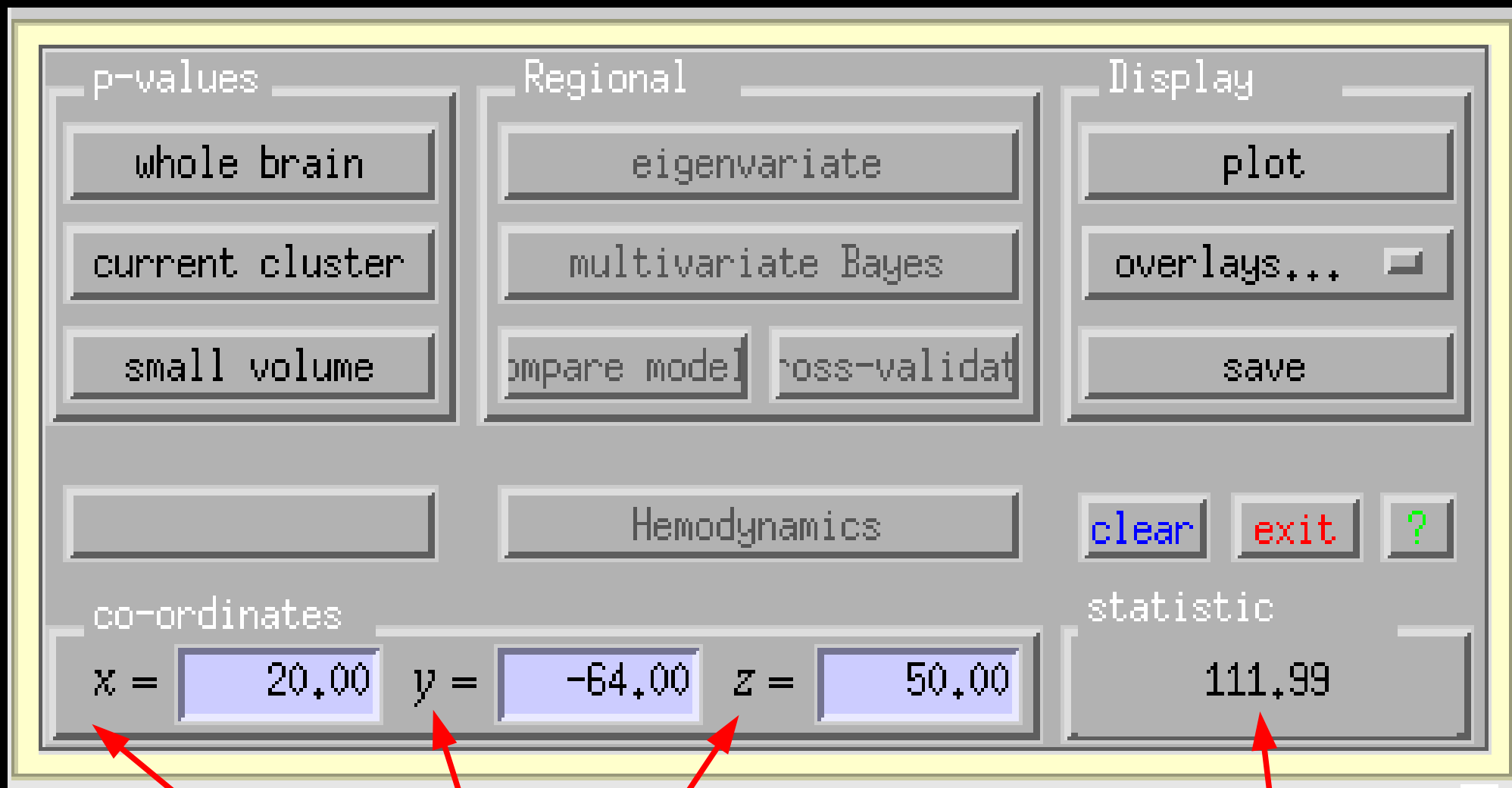
degrés de liberté

SPMresults: .\stats_precalculées_hrf
Height threshold F = 11.716791 (p < 0.05 (FWE))
Extent threshold k = 20 voxels

valeur critique

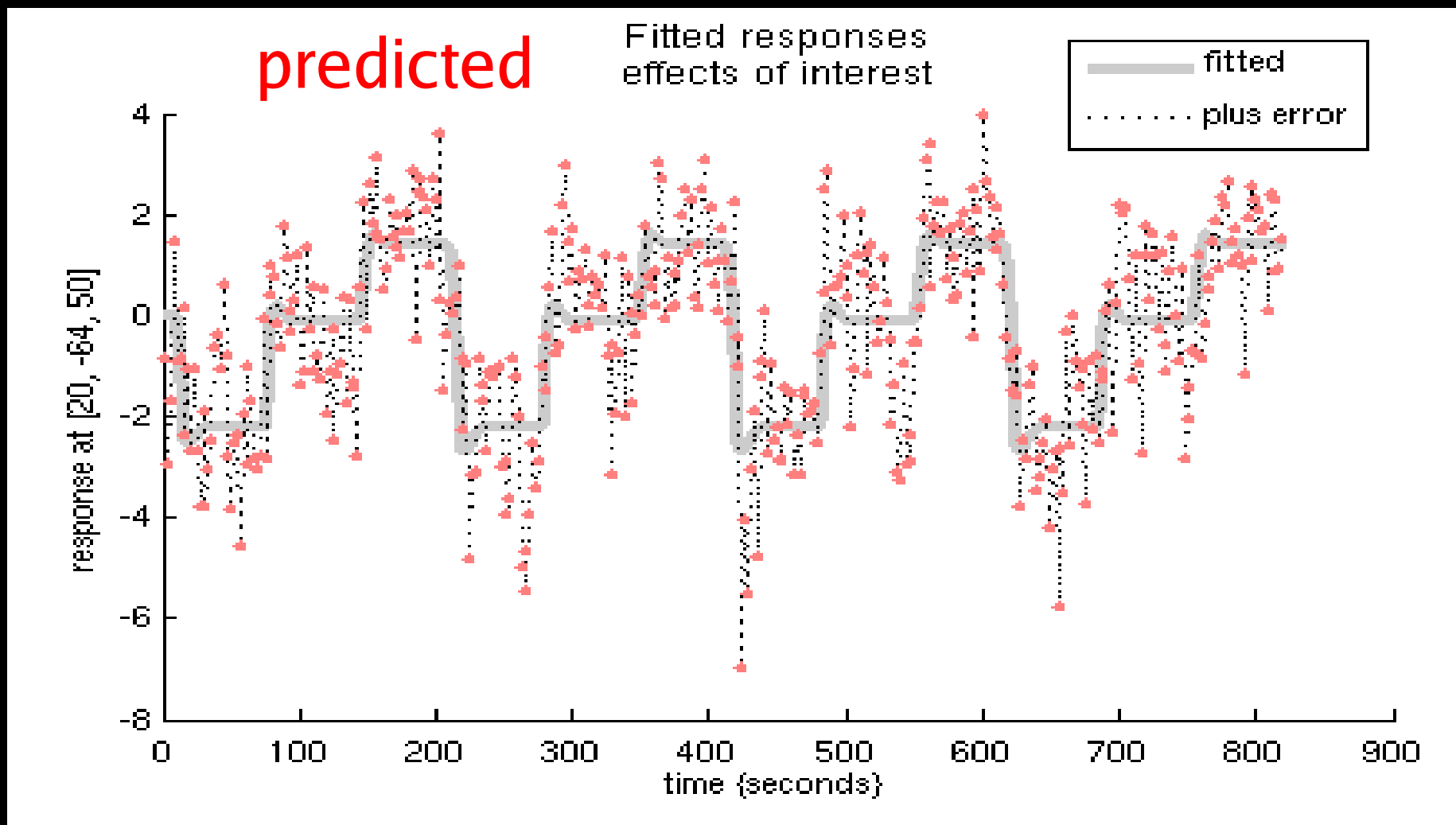
contrast(s)





coordonnées du curseur rouge en mm

valeur de F à la position du curseur

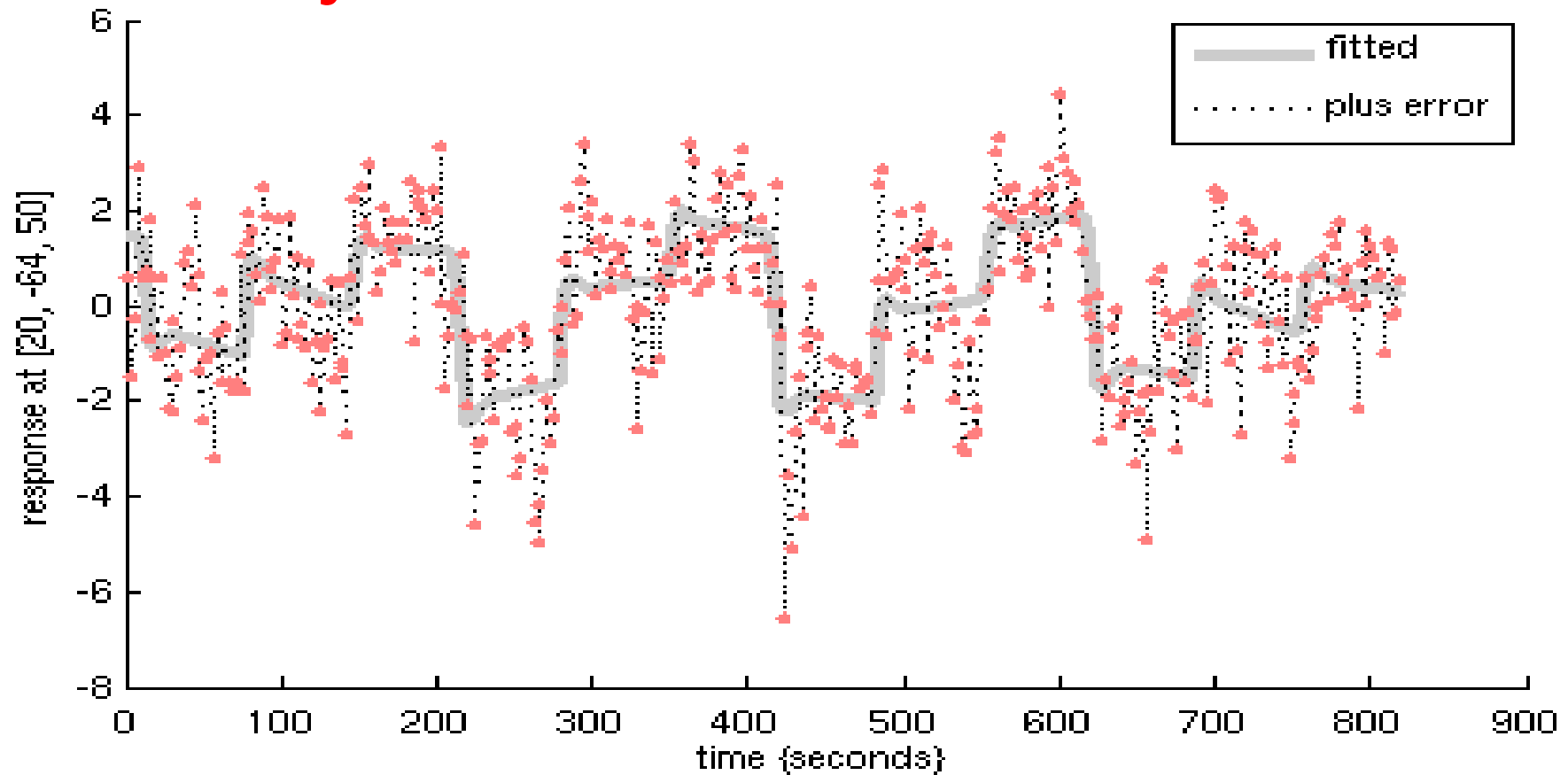


$$\text{fitted} : \hat{P} = \hat{\beta}_0 X_0 + \hat{\beta}_1 X_1 + \hat{\beta}_2 X_2$$

$$\text{plus error} : \hat{P} = \hat{\beta}_0 X_0 + \hat{\beta}_1 X_1 + \hat{\beta}_2 X_2 + \text{erreur} = \text{fit} + (\text{signal} - \text{fit})$$

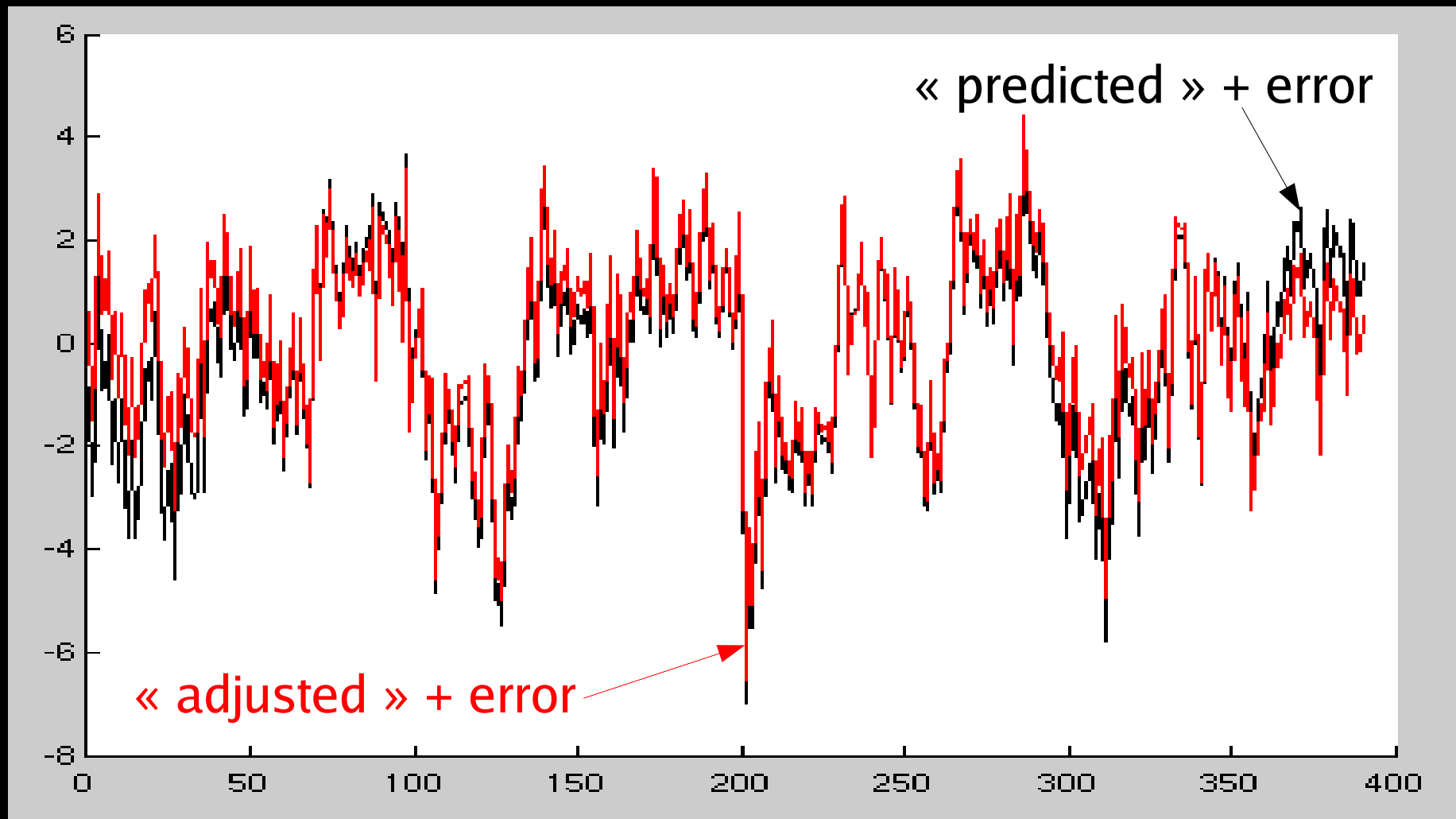
adjusted

Fitted responses
effects of interest

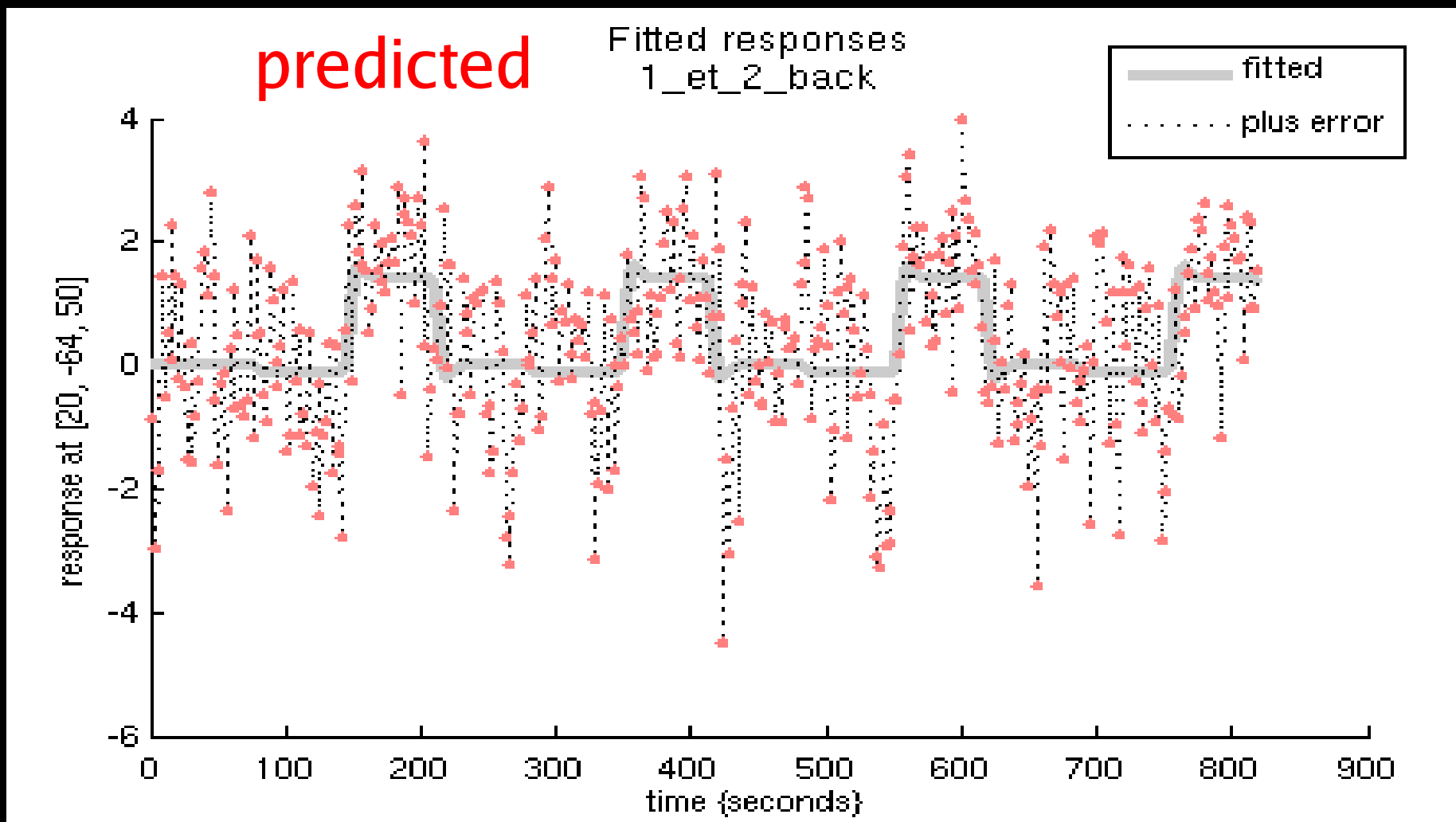


fitted : $\hat{A} = \text{signal mesuré} - \text{erreur}$

plus error : $\hat{A} = (\text{signal mesuré} - \text{erreur}) + \text{erreur}$



c'est t rès proche du « vrai » signal BOLD dans le voxel !

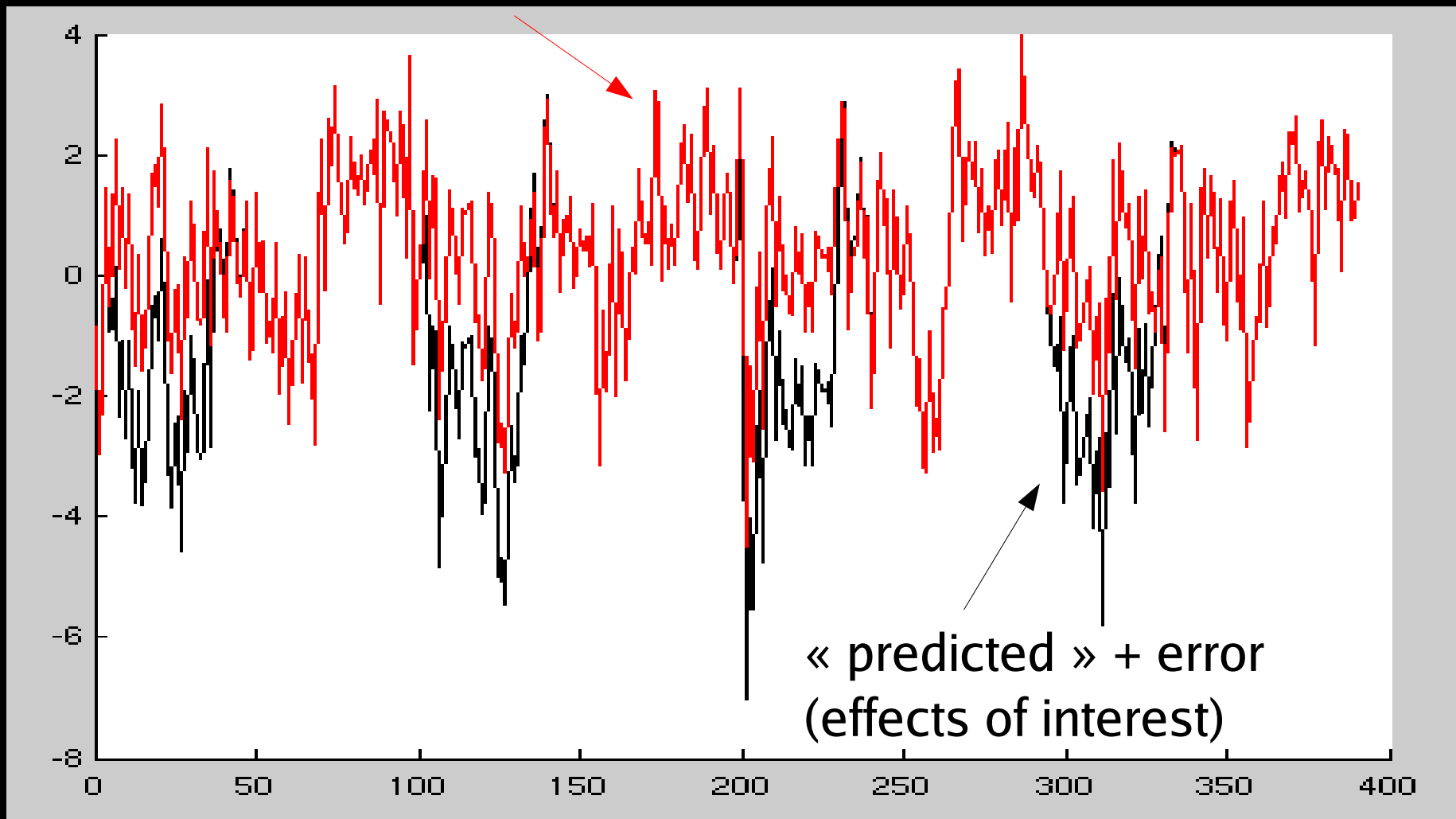


$$\text{fitted} : \hat{P} = \hat{\beta}_1 X_1 + \hat{\beta}_2 X_2$$

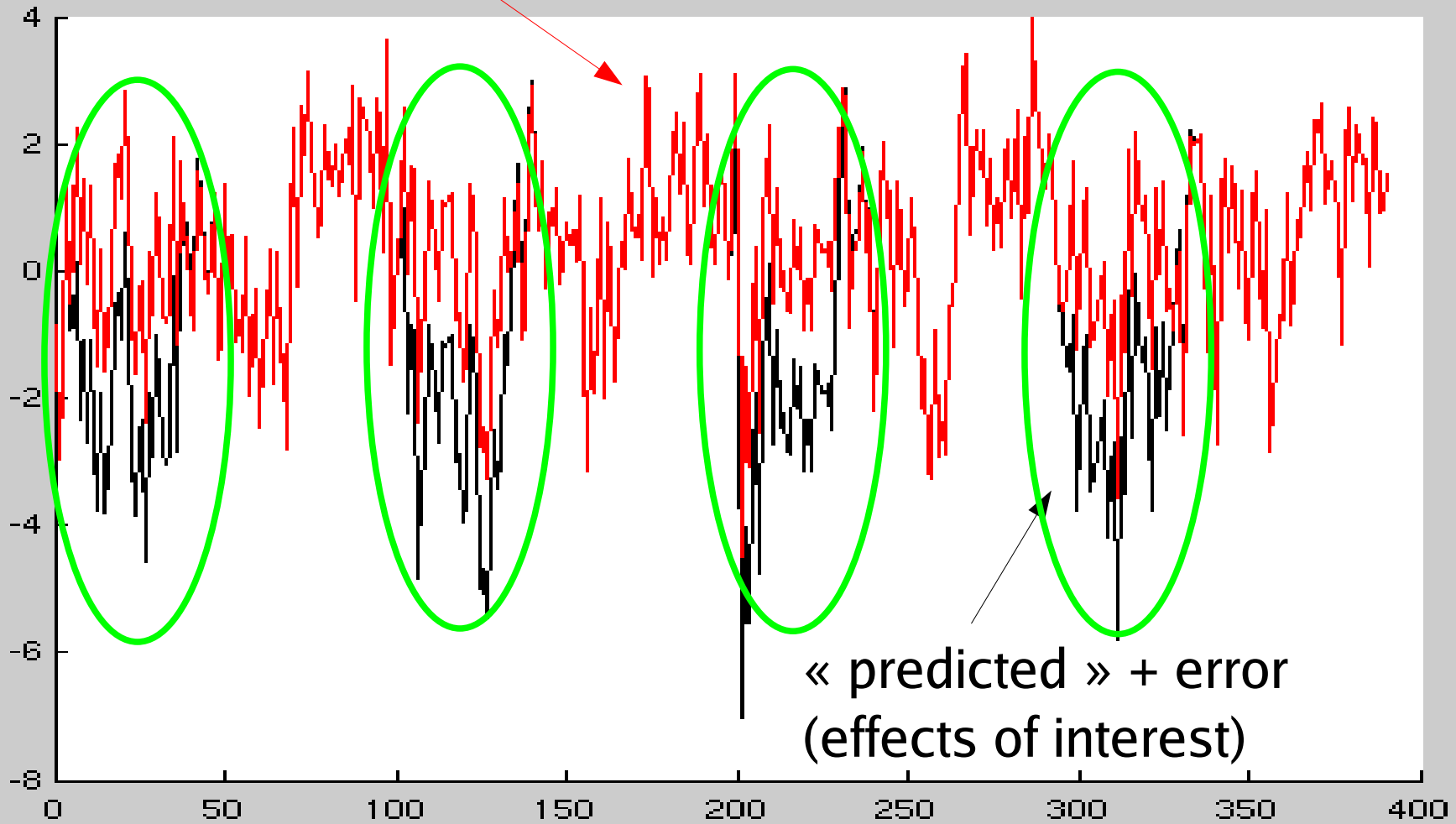
$$\text{plus error} : \hat{P} = \hat{\beta}_1 X_1 + \hat{\beta}_2 X_2 + \text{erreur} = \text{fit} + (\text{signal} - \text{fit} \quad \text{complet})$$

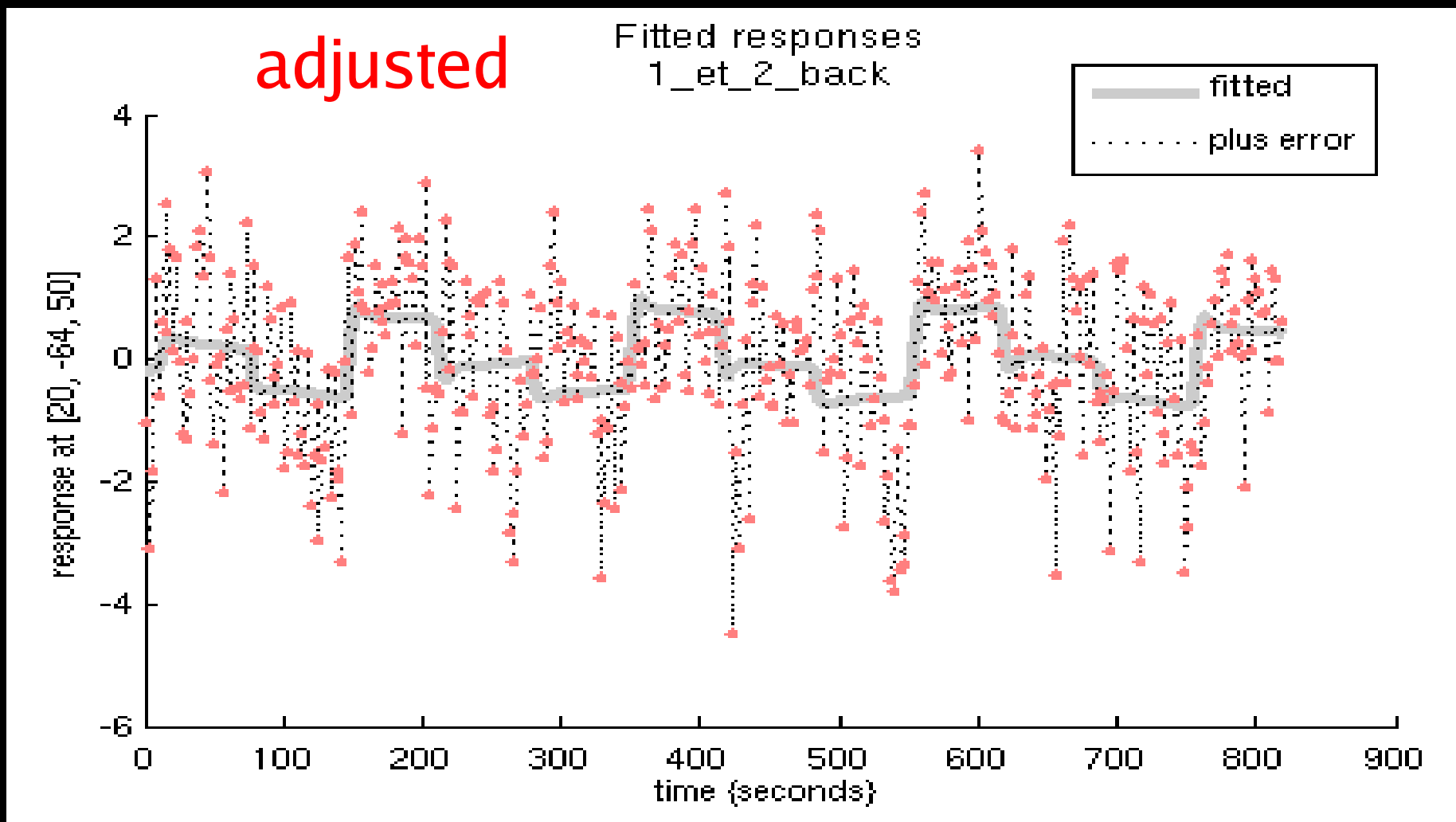
$$= \text{signal} - \beta_0 X_0$$

« predicted » + error
1_et_2_back



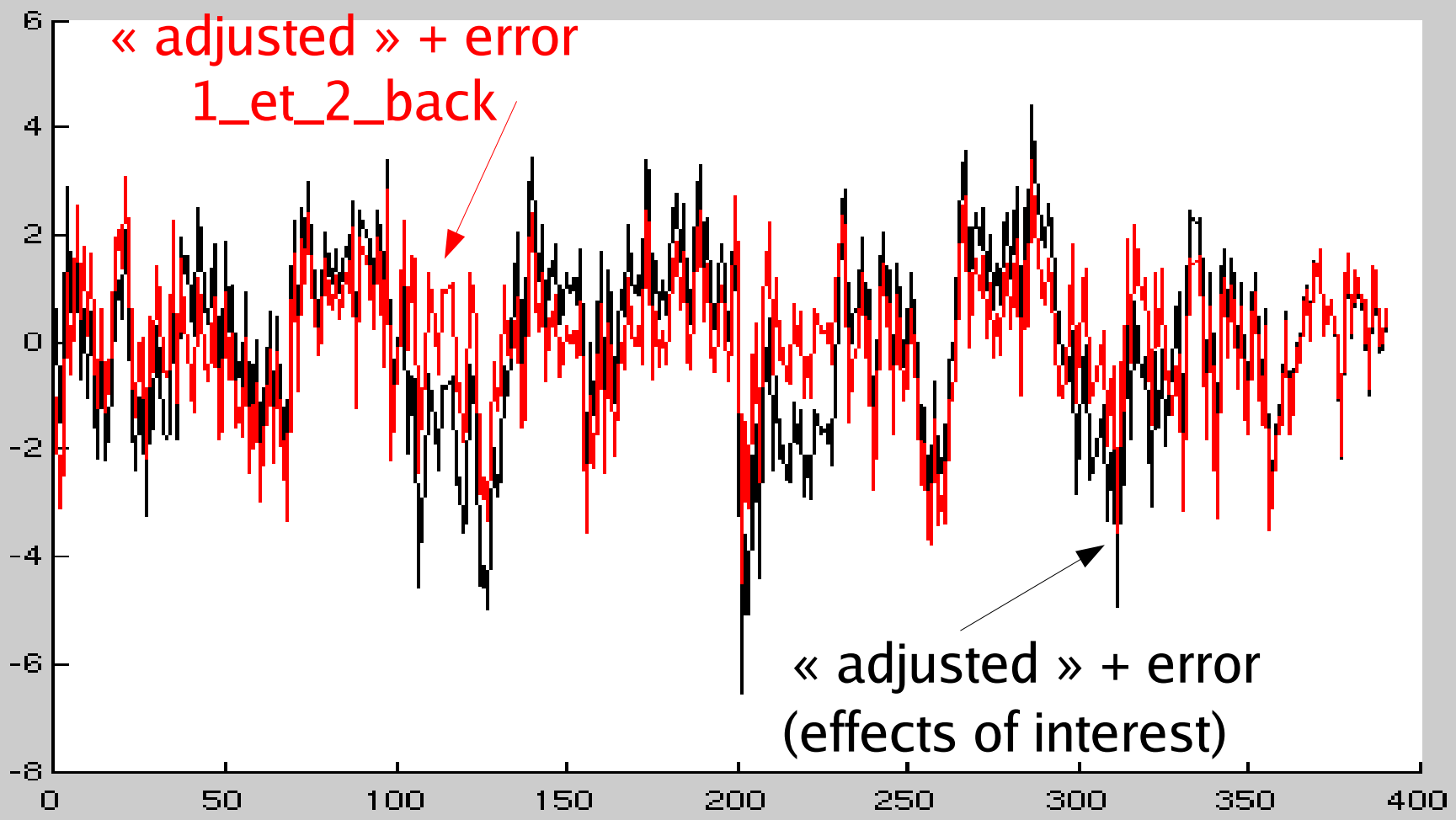
« predicted » + error
1_et_2_back

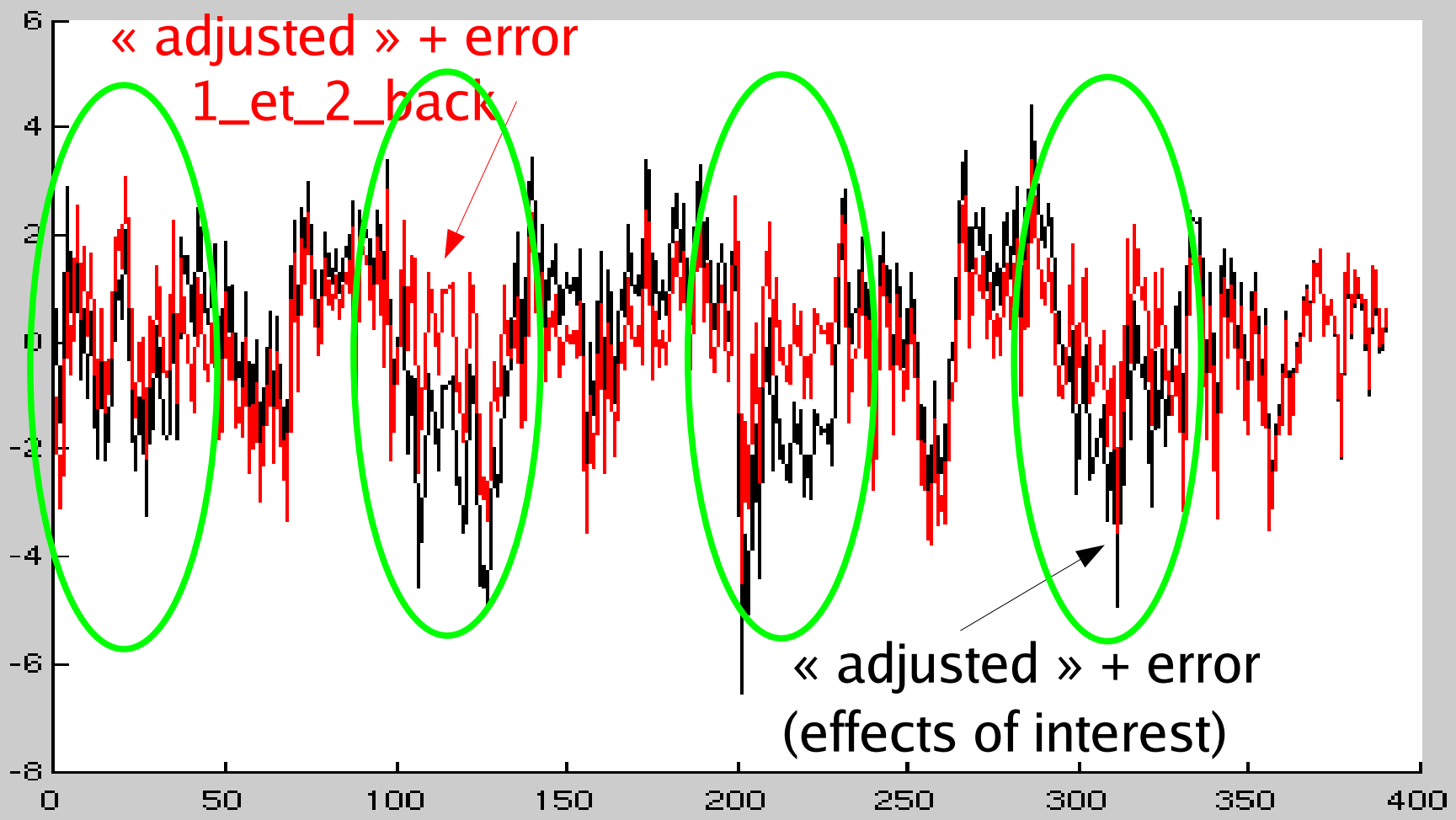




fitted : $\hat{A} = \text{signal mesuré corrigé pour } X_0 - \text{erreur}$

plus error : $\hat{A} = (\text{signal mesuré corrigé pour } X_0 - \text{er reur}) + \text{erreur}$

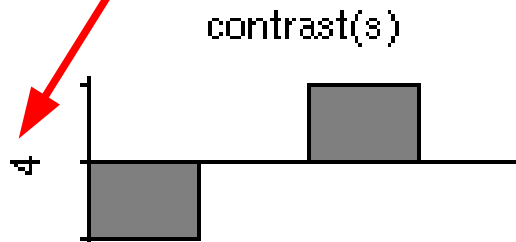
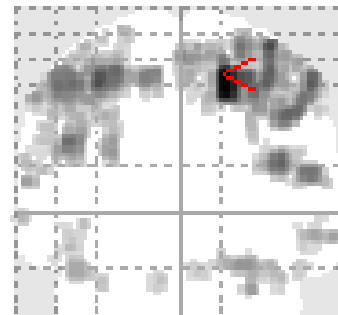
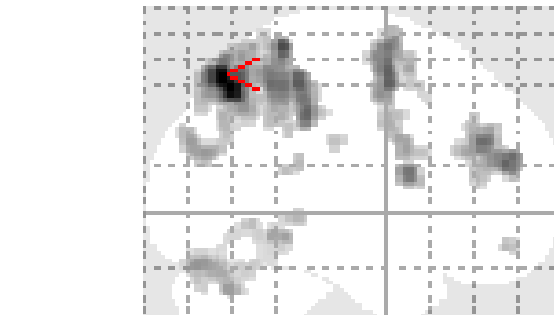




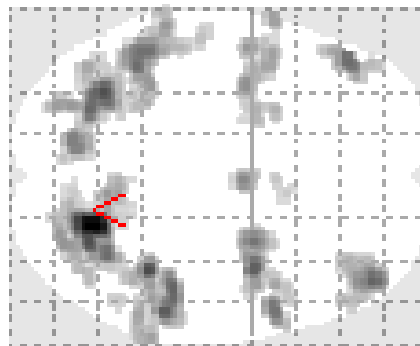
con_0004
spmT_0004

2-back-vs-0-back

numéro du contraste

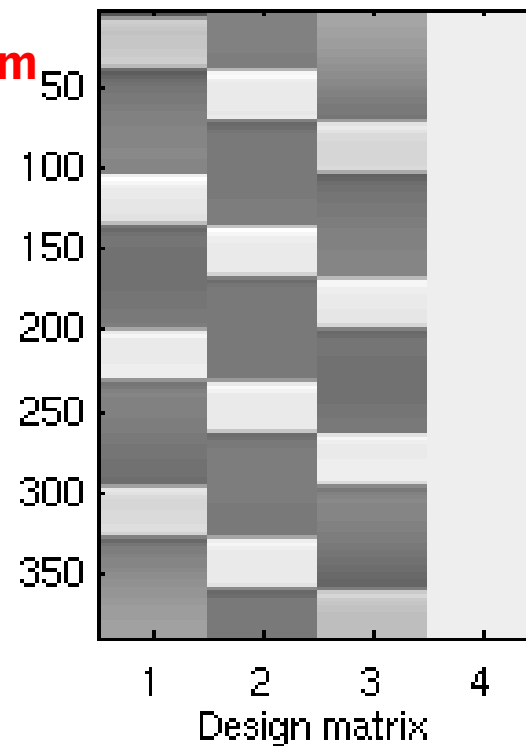


SPM{xip
[20, -64, 50]} ← coordonnées du curseur rouge en mm



SPM{T₃₆₀}

degrés de liberté



SPMresults: .\stats_precalculées_hrf
Height threshold T = 5.128281 (p < 0.05 (FWE))
Extent threshold k = 20 voxels

valeur critique

Statistics: *p-values adjusted for search volume*

set-level		non-isotropic adjusted cluster-level			voxel-level					mm mm mm		
p	c	$p_{corrected}$	k_E	$p_{uncorrected}$	$p_{FWE-corr}$	$p_{FDR-corr}$	T	(Z_{Ξ})	$p_{uncorrected}$			
0.000	21	0.000	1386	0.000	0.000	0.000	18.12	Inf	0.000	20	-64	50
					0.000	0.000	13.48	Inf	0.000	38	-44	66
					0.000	0.000	12.57	Inf	0.000	54	-38	52
		0.000	1090	0.000	0.000	0.000	13.12	Inf	0.000	-34	-62	52
					0.000	0.000	11.80	Inf	0.000	-26	-68	56
					0.000	0.000	11.58	Inf	0.000	-44	-48	52
		0.000	580	0.000	0.000	0.000	12.24	Inf	0.000	38	0	56
					0.000	0.000	11.12	Inf	0.000	26	0	66
					0.000	0.000	8.70	Inf	0.000	26	-4	48
		0.000	247	0.000	0.000	0.000	12.08	Inf	0.000	42	50	20
					0.000	0.000	7.43	7.17	0.000	50	38	14
		0.000	225	0.000	0.000	0.000	11.64	Inf	0.000	-46	40	28
		0.000	104	0.000	0.000	0.000	11.16	Inf	0.000	54	10	16
					0.000	0.000	6.90	6.69	0.000	46	14	24
		0.000	98	0.000	0.000	0.000	10.01	Inf	0.000	2	-4	62
		0.000	268	0.000	0.000	0.000	9.54	Inf	0.000	-36	-2	58
					0.000	0.000	7.79	7.50	0.000	-26	0	60
					0.000	0.000	7.65	7.37	0.000	-26	10	60
		0.000	216	0.000	0.000	0.000	9.34	Inf	0.000	28	-78	-22
					0.000	0.000	8.95	Inf	0.000	30	-64	-32
					0.000	0.000	7.79	7.49	0.000	38	-70	-22
		0.000	89	0.000	0.000	0.000	9.00	Inf	0.000	-28	-76	24
					0.000	0.000	6.00	5.87	0.000	-26	-64	32
		0.000	235	0.000	0.000	0.000	9.00	Inf	0.000	-52	-2	48
					0.000	0.000	8.54	Inf	0.000	-48	8	26
					0.000	0.000	8.06	7.73	0.000	-42	0	36

table shows 3 local maxima more than 8.0mm apart

Height threshold: $T = 5.13$, $p = 0.000$ (0.050) ($p < 0.05$ (FWE)) Degrees of freedom = [1.0, 380.0]
 Extent threshold: $k = 20$ voxels, $p = 0.000$ (0.000) FWHM = 6.1 6.0 6.3 mm mm mm; 3.0 3.0 3.2 (voxels);
 Expected voxels per cluster, $\langle k \rangle = 0.737$ Volume: 1713368; 214171 voxels; 6874.0 resels
 Expected number of clusters, $\langle c \rangle = 0.00$ Voxel size: 2.0 2.0 2.0 mm mm mm; (resel = 28.95 voxels)
 Expected false discovery rate, ≤ 0.00 Page 1

Statistics: *p*-values adjusted for search volume

set-level		non-isotropic adjusted cluster-level			voxel-level					mm mm mm		
<i>p</i>	<i>c</i>	<i>p</i> _{corrected}	<i>k</i> _E	<i>p</i> _{uncorrected}	<i>p</i> _{FWE-corr}	<i>p</i> _{FDR-corr}	<i>T</i>	(<i>Z</i> _≡)	<i>p</i> _{uncorrected}			
0.000	21	0.000	1386	0.000	0.000	0.000	18.12	Inf	0.000	20	-64	50
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		0.000	89	0.000	0.000	0.000	9.00	Inf	0.000	-28	-76	24
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					0.000	0.000	7.65	7.37	0.000	-26	10	60
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					0.000	0.000	7.79	7.50	0.000	-26	0	60
					0.000	0.000	7.65	7.37	0.000	-26	10	60
		0.000	216	0.000	0.000	0.000	9.34	Inf	0.000	28	-78	-22
					0.000	0.000	8.95	Inf	0.000	30	-64	-32
					0.000	0.000	7.79	7.49	0.000	38	-70	-22
		0.000	89	0.000	0.000	0.000	9.00	Inf	0.000	-28	-76	24
					0.000	0.000	6.00	5.87	0.000	-26	-64	32
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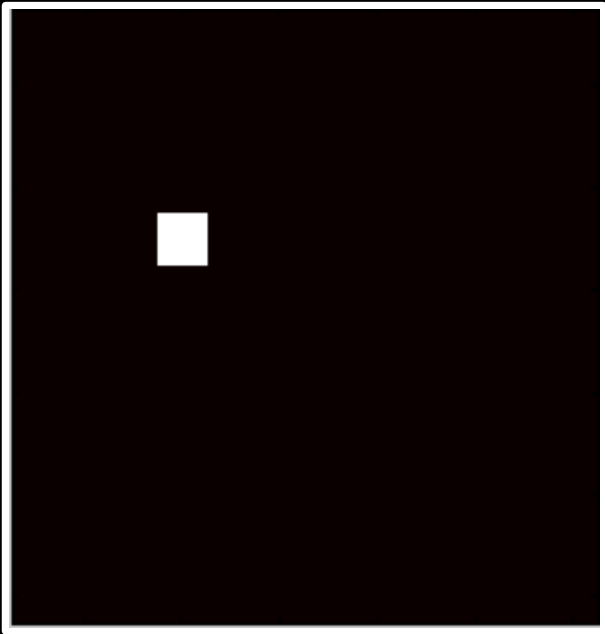
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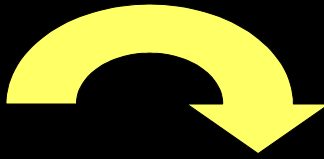
set-level		non-isotropic adjusted cluster-level			voxel-level					mm mm mm		
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					0.000	0.000	13.48	Inf	0.000	38	-44	66
					0.000	0.000	12.57	Inf	0.000	54	-38	52
		0.000	1090	0.000	0.000	0.000	13.12	Inf	0.000	-34	-62	52
					0.000	0.000	11.80	Inf	0.000	-26	-68	56
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		0.000	247	0.000	0.000	0.000	12.08	Inf	0.000	42	50	20
					0.000	0.000	7.43	7.17	0.000	50	38	14
		0.000	225	0.000	0.000	0.000	11.64	Inf	0.000	-46	40	28
		0.000	104	0.000	0.000	0.000	11.16	Inf	0.000	54	10	16
					0.000	0.000	6.90	6.69	0.000	46	14	24
		0.000	98	0.000	0.000	0.000	10.01	Inf	0.000	2	-4	62
		0.000	268	0.000	0.000	0.000	9.54	Inf	0.000	-36	-2	58
					0.000	0.000	7.79	7.50	0.000	-26	0	60
					0.000	0.000	7.65	7.37	0.000	-26	10	60
		0.000	216	0.000	0.000	0.000	9.34	Inf	0.000	28	-78	-22
					0.000	0.000	8.95	Inf	0.000	30	-64	-32
					0.000	0.000	7.79	7.49	0.000	38	-70	-22
		0.000	89	0.000	0.000	0.000	9.00	Inf	0.000	-28	-76	24
					0.000	0.000	6.00	5.87	0.000	-26	-64	32
		0.000	235	0.000	0.000	0.000	9.00	Inf	0.000	-52	-2	48
					0.000	0.000	8.54	Inf	0.000	-48	8	26
					0.000	0.000	8.06	7.73	0.000	-42	0	36

table shows 3 local maxima more than 8.0 resels

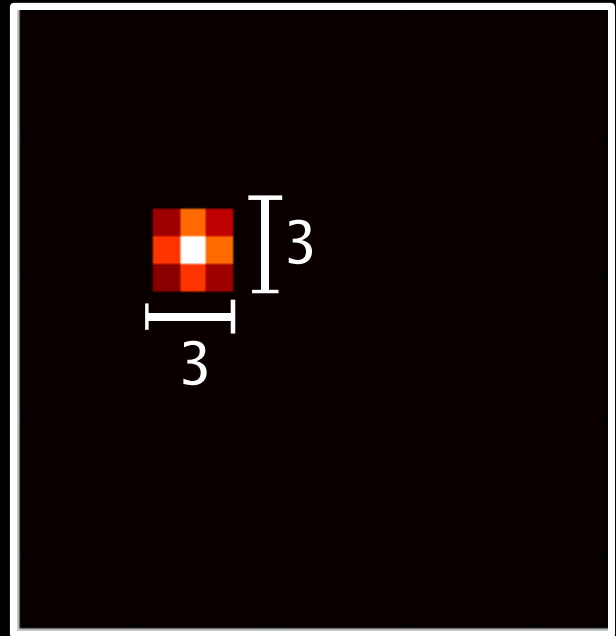
Height threshold: $T = 5.13$, $p = 0.000$ (0.050) ($p < 0.05$ (FWE)) Degrees of freedom = [1.0, 380.0]
 Extent threshold: $k = 20$ voxels, $p = 0.000$ (0.000)
 Expected voxels per cluster, $\langle k \rangle = 0.737$
 Expected number of clusters, $\langle c \rangle = 0.00$
 Expected false discovery rate, ≤ 0.00
 FWHM = 6.1 6.0 6.3 mm mm mm; 3.0 3.0 3.2 (voxels);
 Volume: 1713368; 214171 voxels; 6874.0 resels
 Voxel size: 2.0 2.0 2.0 mm mm mm; (resel = 28.95 voxels)



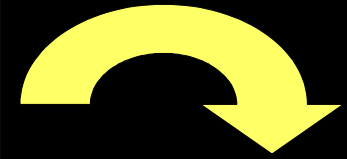
taille du pixel
3,75 x 3,75 mm



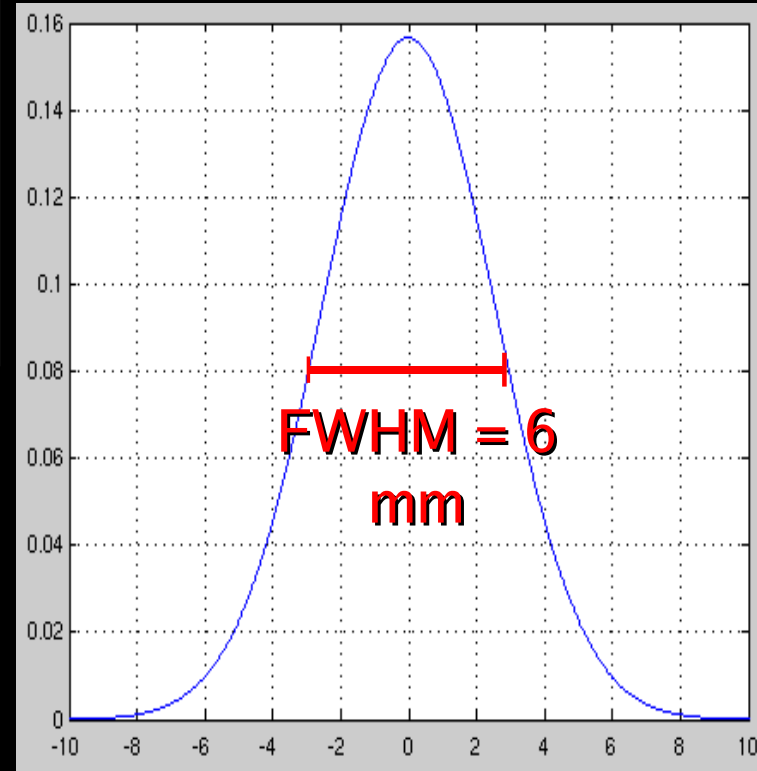
rééchantillonnage
après normalisation



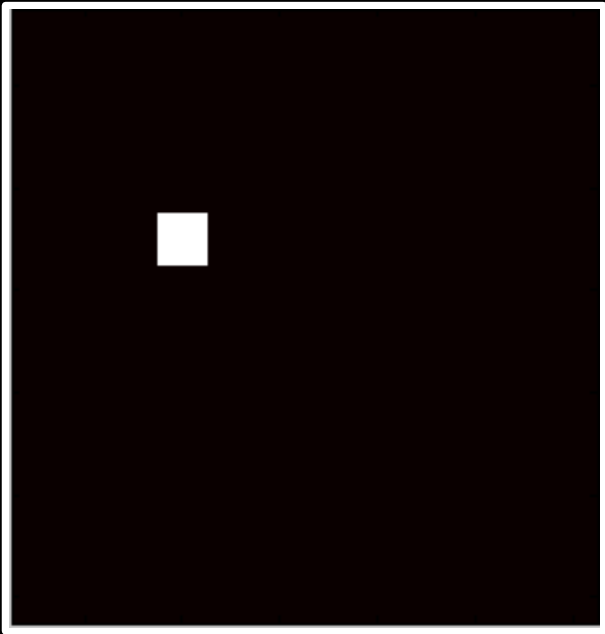
taille du pixel
2 x 2 mm
agrégat : 9 voxels



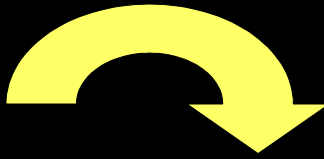
lissage
FWHM = 6 mm * 6 mm



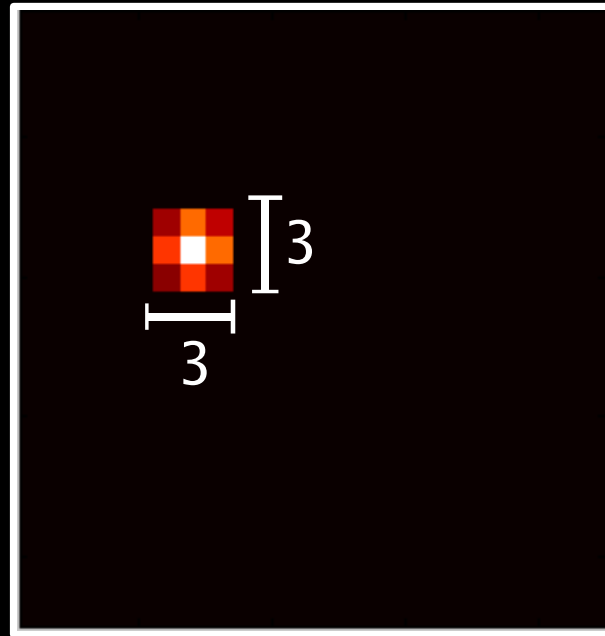
distance en



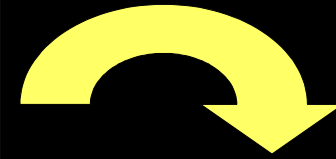
taille du pixel
3,75 x 3,75 mm



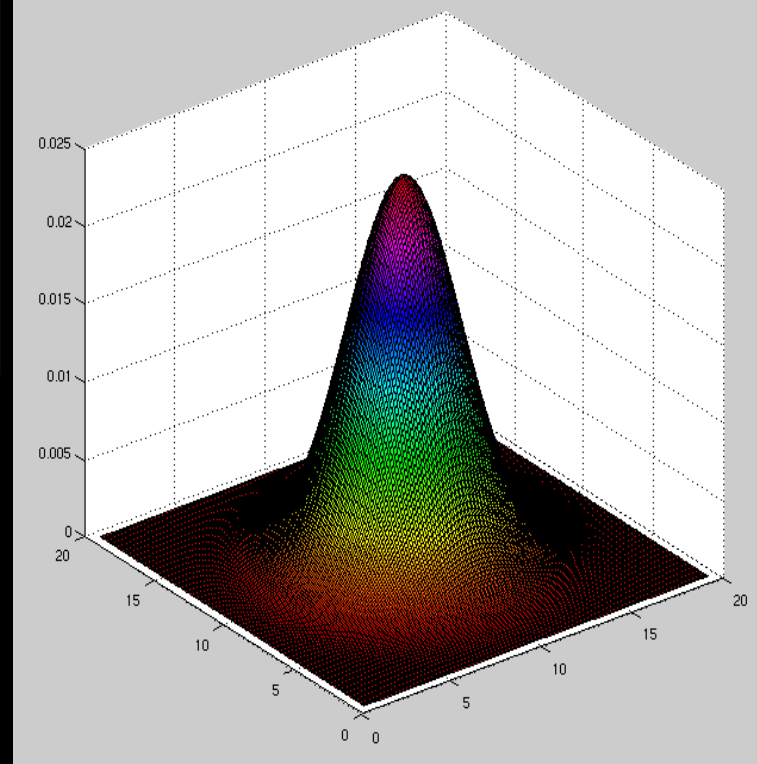
rééchantillonnage
après normalisation

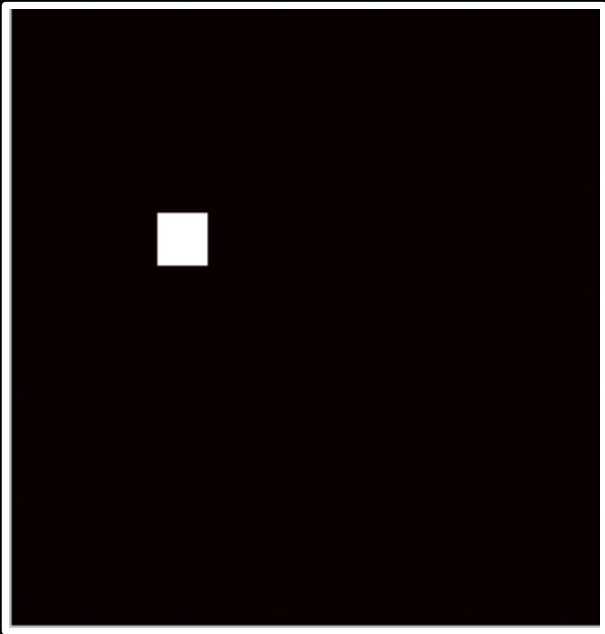


taille du pixel
2 x 2 mm
agrégat : 9 voxels

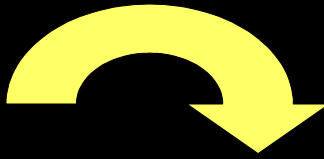


lissage
FWHM = 6 mm * 6 mm

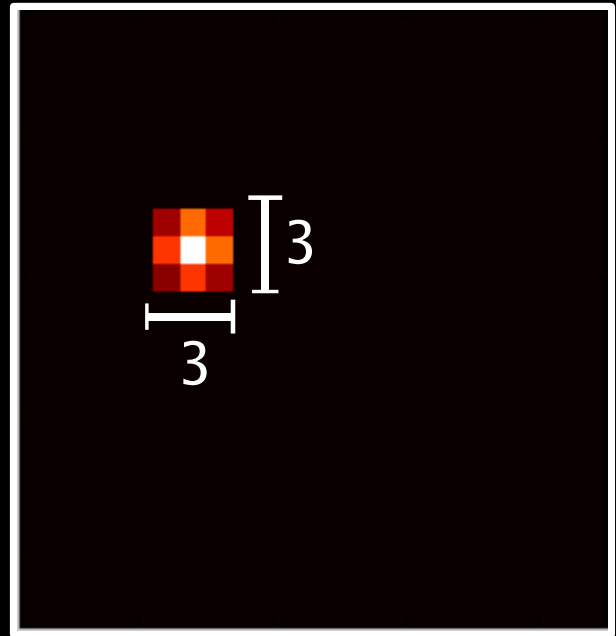




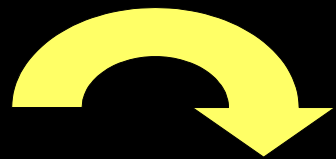
taille du pixel
3,75 x 3,75 mm



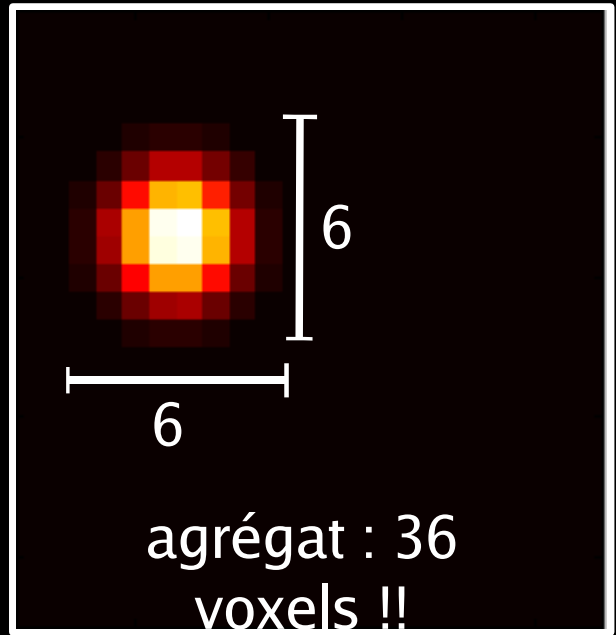
rééchantillonnage
après normalisation



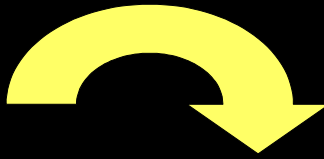
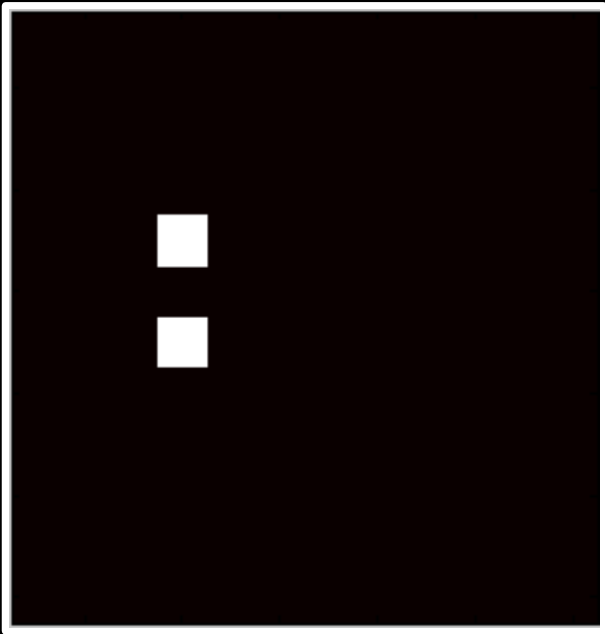
taille du pixel
2 x 2 mm
agrégat : 9 voxels



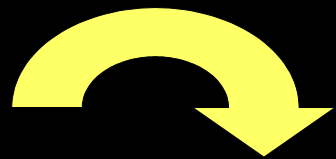
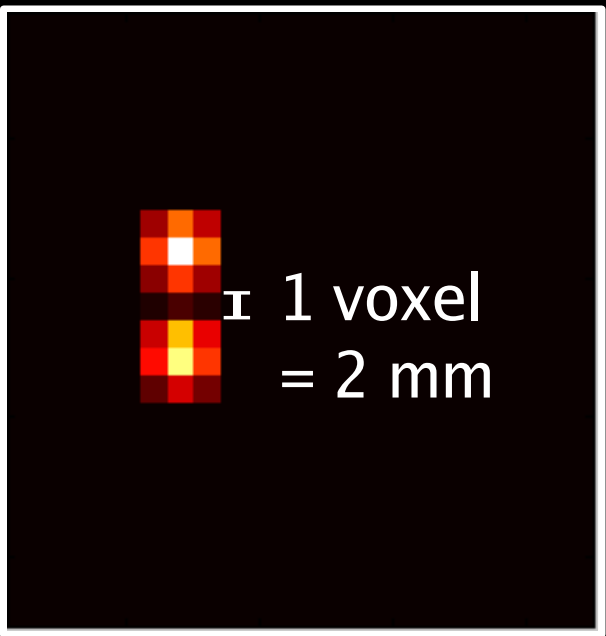
lissage
FWHM = 6 mm * 6 mm



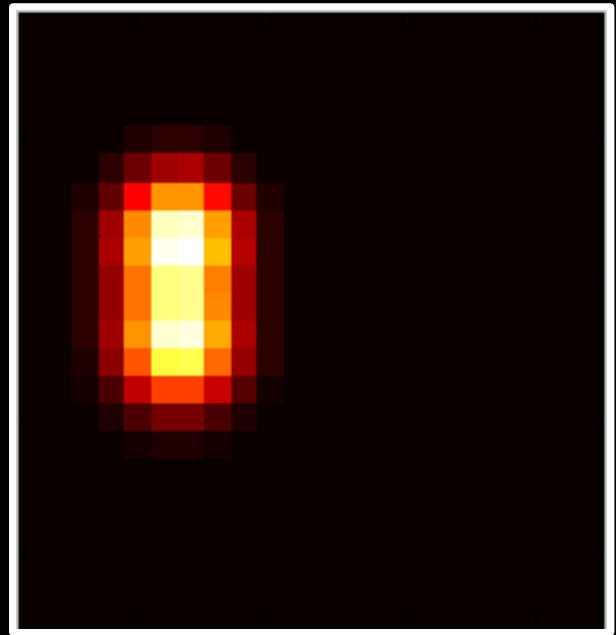
agrégat : 36
voxels !!

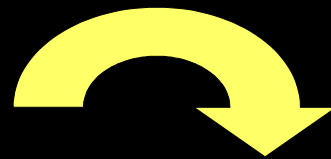
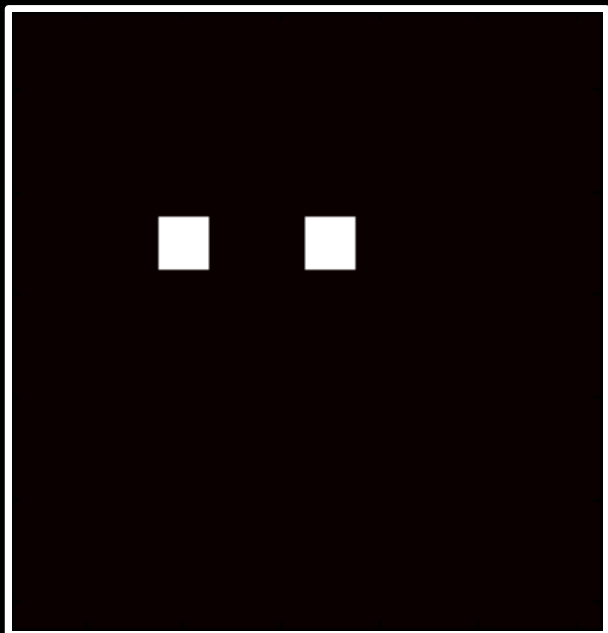


rééchantillonnage
après normalisation

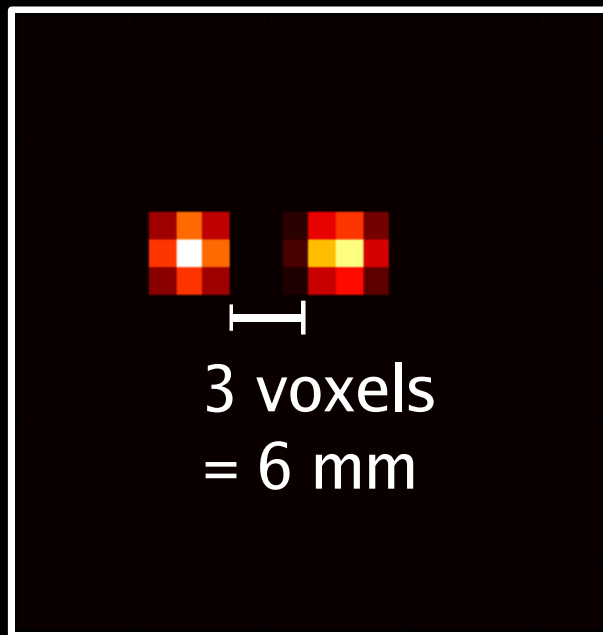


lissage
FWHM = 6 mm * 6 mm

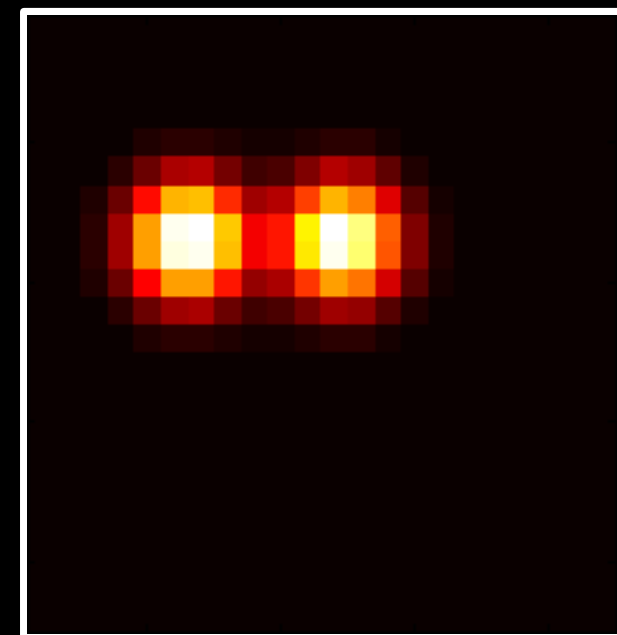
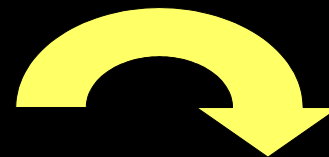




rééchantillonnage
après normalisation



lissage
FWHM = 6 mm * 6 mm



Résolution spatiale ~ FWHM !!!

Statistics: *p*-values adjusted for search volume

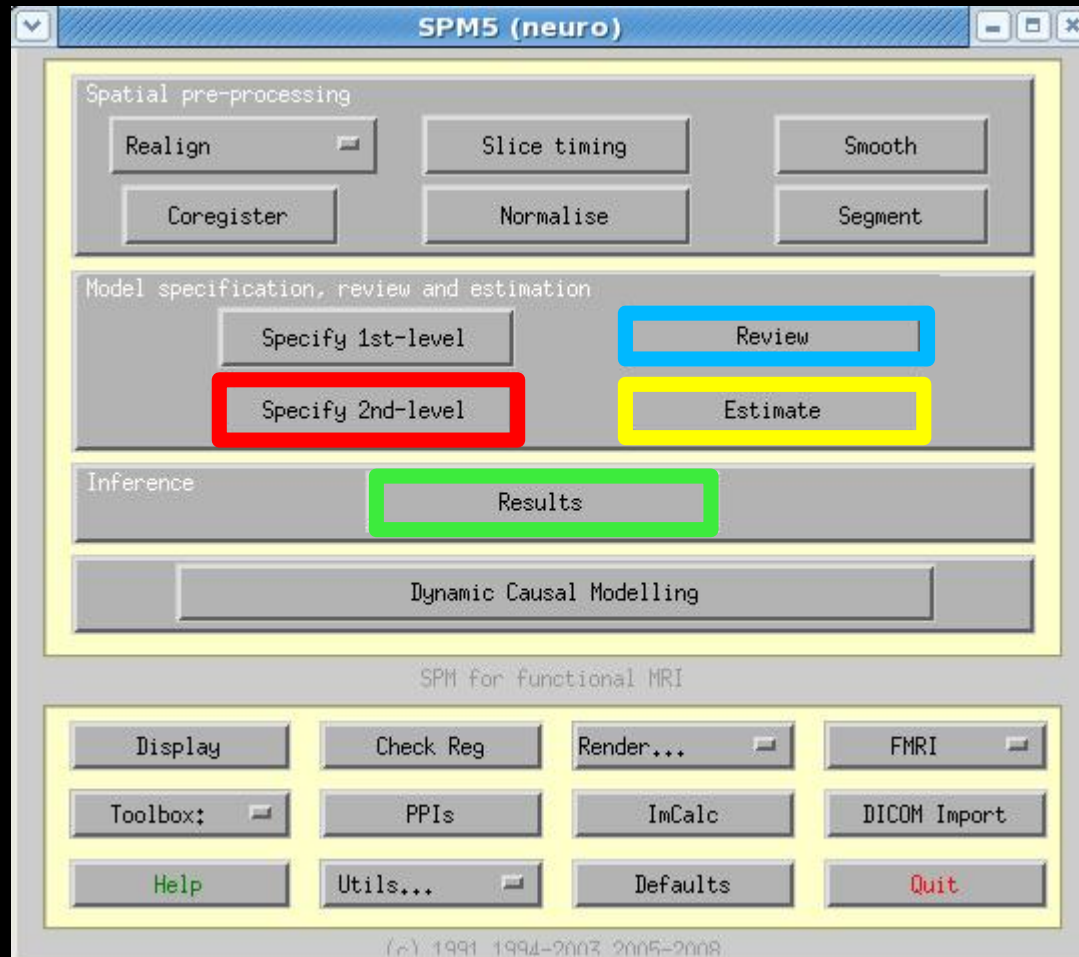
set-level		non-isotropic adjusted cluster-level			voxel-level					mm mm mm		
<i>p</i>	<i>c</i>	<i>p</i> _{corrected}	<i>k</i> _E	<i>p</i> _{uncorrected}	<i>p</i> _{FWE-corr}	<i>p</i> _{FDR-corr}	<i>T</i>	(<i>Z</i> _≡)	<i>p</i> _{uncorrected}			
0.000	21	0.000	1386	0.000	0.000	0.000	18.12	Inf	0.000	20	-64	50
					0.000	0.000	13.48	Inf	0.000	38	-44	66
					0.000	0.000	12.57	Inf	0.000	54	-38	52
		0.000	1090	0.000	0.000	0.000	13.12	Inf	0.000	-34	-62	52
					0.000	0.000	11.80	Inf	0.000	-26	-68	56
					0.000	0.000	11.58	Inf	0.000	-44	-48	52
		0.000	580	0.000	0.000	0.000	12.24	Inf	0.000	38	0	56
					0.000	0.000	11.12	Inf	0.000	26	0	66
					0.000	0.000	8.70	Inf	0.000	26	-4	48
		0.000	247	0.000	0.000	0.000	12.08	Inf	0.000	42	50	20
					0.000	0.000	7.43	7.17	0.000	50	38	14
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					0.000	0.000	6.90	6.69	0.000	46	14	24
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					0.000	0.000	8.95	Inf	0.000	30	-64	-32
					0.000	0.000	7.79	7.49	0.000	38	-70	-22
		0.000	89	0.000	0.000	0.000	9.00	Inf	0.000	-28	-76	24
					0.000	0.000	6.00	5.87	0.000	-26	-64	32
		0.000	235	0.000	0.000	0.000	9.00	Inf	0.000	-52	-2	48
					0.000	0.000	8.54	Inf	0.000	-48	8	26
					0.000	0.000	8.06	7.73	0.000	-42	0	36

table shows 3 local maxima more than 8.0mm apart

Height threshold: $T = 5.13$, $p = 0.000$ (0.050) ($p < 0.05$ (FWE)) Degrees of freedom = [1.0, 380.0]
 Extent threshold: $k = 20$ voxels, $p = 0.000$ (0.000) FWHM = 6.1 6.0 6.3 mm mm mm; 3.0 3.0 3.2 (voxels);
 Expected voxels per cluster, $\langle k \rangle = 0.737$ Volume: 1713368; 214171 voxels; 6874.0 resels
 Expected number of clusters, $\langle c \rangle = 0.00$ Voxel size: 2.0 2.0 2.0 mm mm mm; (resel = 28.95 voxels)
 Expected false discovery rate, ≤ 0.00 Page 1



Analyse de second niveau



1- Décrire X

4 - Faire des tests (inférence) sur les β

2- Vérifier X

3- Estimer β